

## p. 602 Magnetars + Soft Gamma Repeaters

Magnetar = ns wr  $B \sim 10^{11} T$ ,  $P = 5-8s$ , may be source of SGRs (soft gamma-ray repeaters),  
 Correlated wr young ( $\sim 10^4$  yr) SNRs.  
 Emission mechanism - B-field stresses cause crust to crack, resulting in huge release of energy.

## Ch. 17 General Relativity + Black Holes

### §17.1 The General Theory of Relativity p. 609

Newtonian gravity  $F = G \frac{Mm}{r^2}$  worked fine, except for an inconsistency in the perihelion shift of Mercury (Fig 17.1)

Perihelion shifts by  $574''/\text{century}$ ,  $43''$  more than predicted by Newtonian grav.  
 GR is a more accurate theory of gravity + predicts it correctly.

#### The Curvature of Spacetime

Special Relativity (SR) is special in dealing only w/ constant velocity  
 GR was developed by Einstein in 1907-15

GR is a geometric theory. (Fig 17.2 p. 611) Mass curves spacetime + curved spacetime tells mass how to move.

Gravity also bends the path of light (Fig. 17.3 p. 611)

Spacetime is curved thru 4<sup>th</sup> spatial dimension. Light takes shortest path in this curved spacetime (Fig 17.4 p. 612)

Dotted line ACB in Fig. 3 + 4 looks shorter, but is actually longer. Also, time runs slower at point C - both effects contribute equally to making the solid line the shorter (time) path.

GR has been experimentally verified.

AE himself did the calculations of the perihelion shift of Mercury.

"For a few days, I was beside myself with joyous excitement"  
 Light-bending was measured by Arthur Eddington in the solar eclipse of 1919. ( $1.75''$ ) (Fig. 17.5 p. 613)

### p. 613 The Principle of Equivalence

There are 2 kinds of mass - inertial mass  $F = M_i a$  + gravitational mass  $F_g = G \frac{M M_g}{r^2}$ .

It is an experimental fact that  $M_i = M_g$  to 1 part in  $10^{12}$ , but this is inexplicable in Newtonian mechanics.

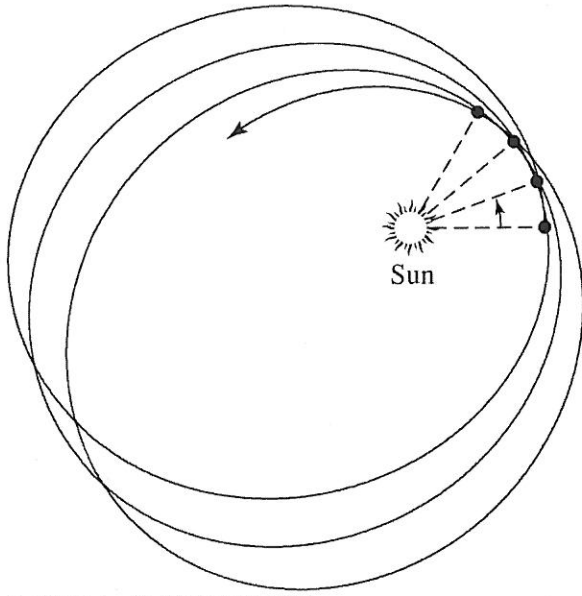


Fig. 17.1 Perihelion shift of Mercury (exaggerated)

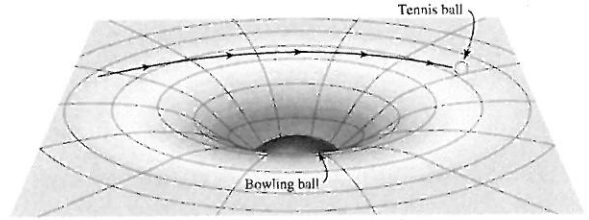


Fig. 17.2 Rubber sheet analogy for curved space around Sun

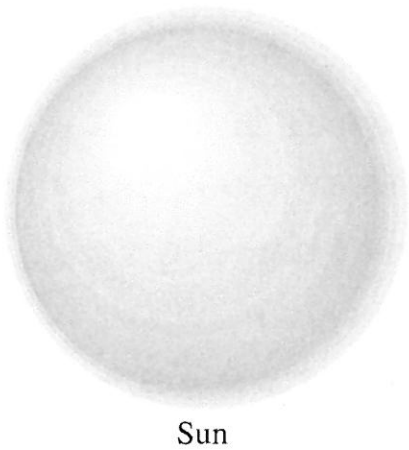
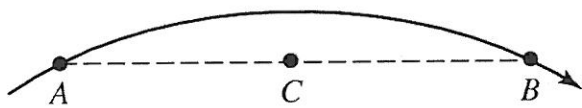


Fig. 17.3 Photon's path around Sun (curvature exaggerated).

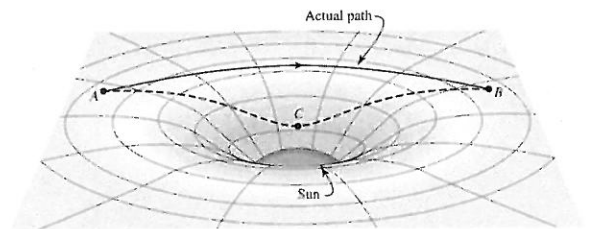


Fig. 17.4 Two photon paths. ACB is the projection of ACB from Fig. 17.3.

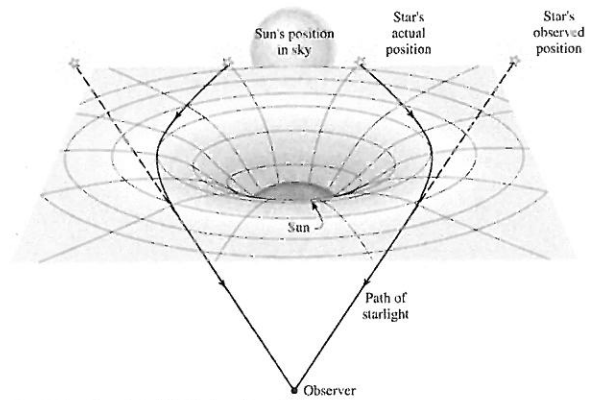


Fig. 17.5 Bending of starlight during solar eclipse.



GR is based on Einstein's "happiest thought" of 1907 "If a person falls freely he does not feel his own weight."

(Fig. 17.6 p. 615) Gravity is equivalent to an accelerating laboratory.

(Fig. 17.7 p. 616)

(Fig. 17.8) Must use local inertial frames, small enough that  $\vec{g} \approx \text{const.}$  inside.

Principle of Equivalence: All local, freely falling, nonrotating laboratories are fully equivalent for the performance of all physical experiments.

p. 617 The Bending of Light

(Fig. 17.9) Photon fired horizontally in freely falling lab - falls distance  $d = \frac{1}{2}gt^2 \Rightarrow$  deflection  $\angle \theta = \frac{gd}{c^2} = 10^{-15}$  rad for  $l = 10$  m, (17.10)

p. 619 Gravitational Redshift & Time Dilation

This time let the photon be fired upwards in the freely falling laboratory. (Fig. 17.11)

In the falling frame gravity is abolished, so a frequency meter in the ceiling measures the same frequency  $\nu_0$ .

Ground observer  $\Rightarrow$  light traveled time  $t = h/c \Rightarrow$  reached speed  $gt = \frac{gh}{c}$

$\Rightarrow$  should have experienced blue-shift  $\frac{\Delta\nu}{\nu_0} = \frac{\nu}{c} = \frac{gh}{c^2}$ .

But there was no change in frequency  $\Rightarrow$  must be another effect.

Gravitational redshift  $\frac{\Delta\nu}{\nu_0} = -\frac{gh}{c^2}$

Outside observer observes only the gravitational redshift.

If light travels downwards, it's a blue shift.

Ex. 17.1.1 p. 620 Tested at Harvard in 1960.  $\gamma$ -rays emitted from bottom of 22.6 m tower.

$$\Delta\nu/\nu_0 = -gh/c^2 = -9.8 \text{ m/s}^2 \cdot 22.6 \text{ m} / (3 \times 10^8 \text{ m/s})^2 = -2.46 \times 10^{-15}$$

Experimental result  $\Delta\nu/\nu_0 = -(2.57 \pm 0.26) \times 10^{-15}$

For photon traveling outwards to infinity get  $\int_{\nu_0}^{\nu_\infty} \frac{d\nu}{\nu} = -\int_{r_0}^{\infty} \frac{g dr}{c^2}$

$$= -\int_{r_0}^{\infty} \frac{GM}{r^2 c^2} dr \Rightarrow \ln \frac{\nu_\infty}{\nu_0} = -\frac{GM}{r_0 c^2} \Rightarrow$$

$$\frac{\nu_\infty}{\nu_0} = e^{-GM/r_0 c^2} \approx 1 - \frac{GM}{r_0 c^2} \quad \left(\frac{GM}{r_0 c^2} \ll 1\right)$$

Not exact, because all  $dr$ 's are in different frames.

Exact  $\nu_\infty/\nu_0 = (1 - 2GM/r_0 c^2)^{1/2}$

Redshift parameter defined in ch. 4:

$$z = \frac{\lambda_\infty - \lambda_0}{\lambda_0} = \frac{\nu_0}{\nu_\infty} - 1 = (1 - \frac{2GM}{r_0 c^2})^{-1/2} - 1 \approx \frac{GM}{r_0 c^2} \quad \left(\text{if } \frac{GM}{r_0 c^2} \ll 1\right)$$

Let  $\Delta t$  be the time for a complete oscillation of wave of frequency  $\nu$ ,  $\Delta t = \nu^{-1}$ .

$$\frac{\Delta t_0}{\Delta t_\infty} = \frac{\nu_\infty}{\nu_0} = (1 - \frac{2GM}{r_0 c^2})^{1/2} \approx 1 - \frac{GM}{r_0 c^2} \quad (\text{weak field})$$

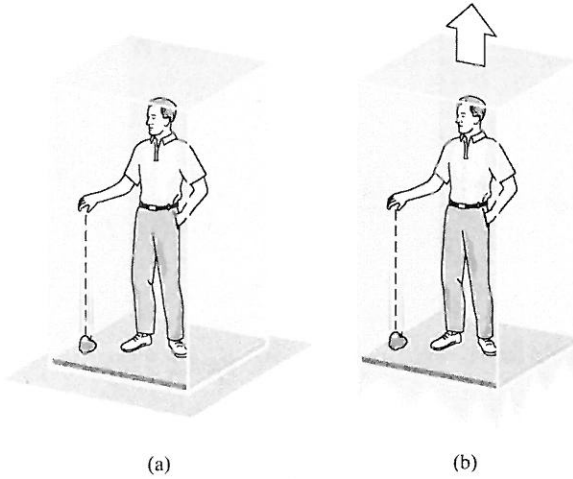


Fig. 17.6 Gravity is equivalent to accelerating laboratory.

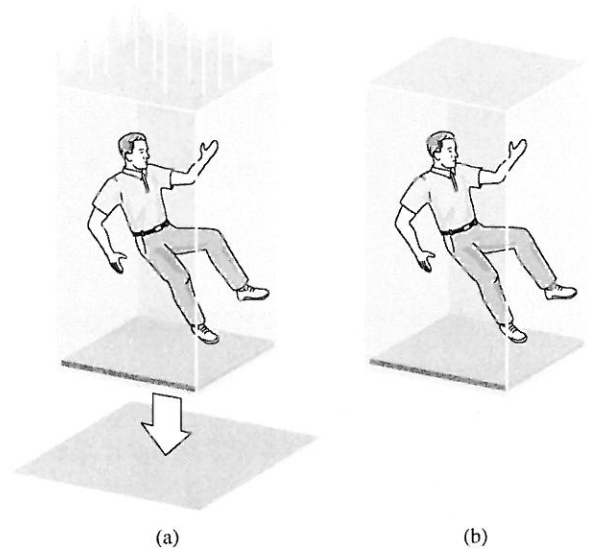


Fig. 17.7 Gravity abolished in freely falling laboratory.

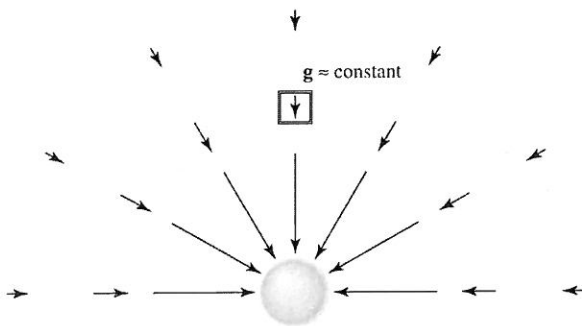


Fig. 17.8 Local inertial frame w/  $g \approx$  constant inside.

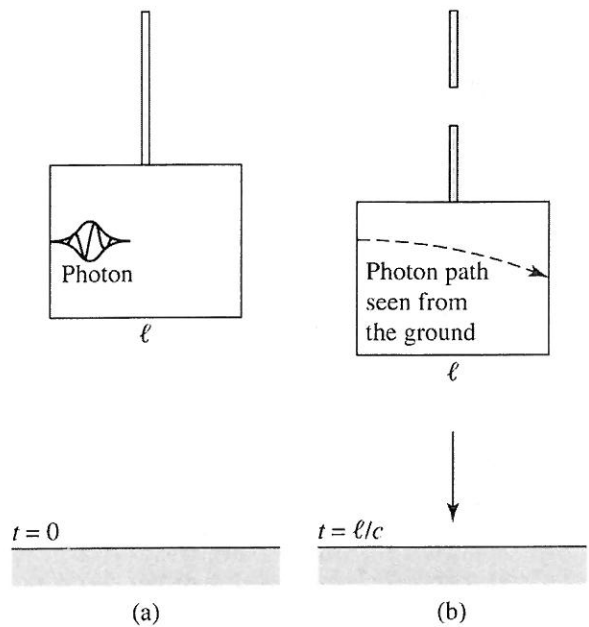


Fig. 17.9 Equivalence principle for horizontally traveling photon.

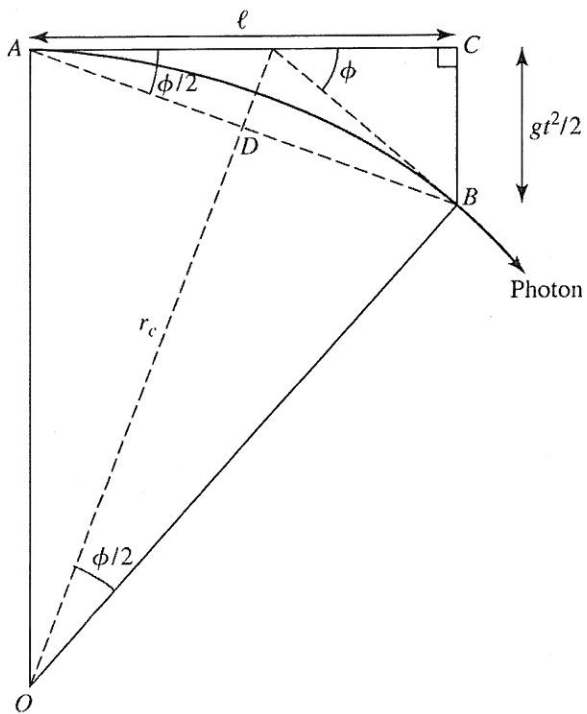


Fig. 17.10 Geometry for radius of curvature  $r_c$  & angular deflection  $\phi$ .

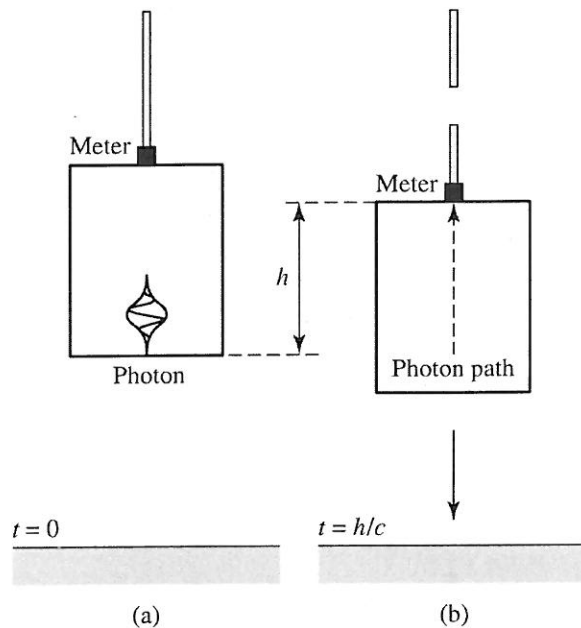


Fig. 17.11 Equivalence principle for vertically traveling photon.

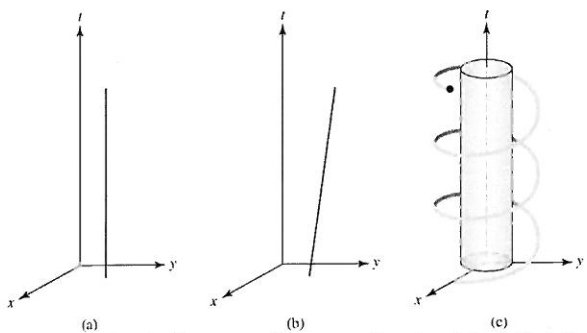


Fig. 17.12 Worldlines for (a) man at rest, (b) woman running w/ constant  $v$ , & (c) satellite orbiting Earth.

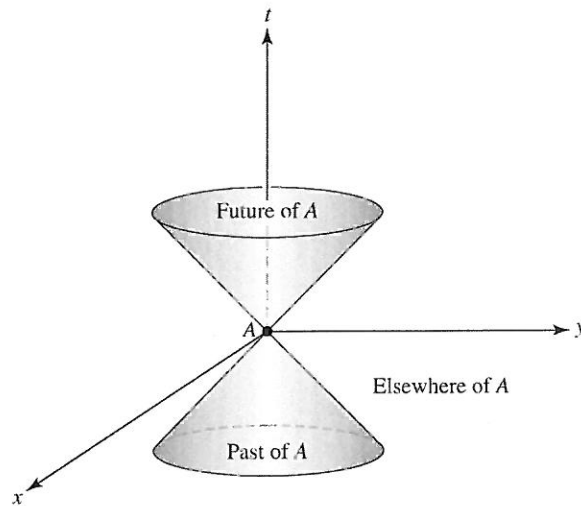


Fig. 17.13 Light cones generated by horizontally traveling photons emitted at  $t = 0$ .



This is gravitational time dilation - time runs slower in a grav. field.  
2 identical clocks side by side, One lowered into grav well & brought back up - it will be behind.

Ex. 17.1.2 p. 622 Sirius B,  $R = 5.5 \times 10^6 \text{ m}$ ,  $M = 2.1 \times 10^{30} \text{ kg}$   
 $\Phi = GM/Rc^2 = 2.8 \times 10^{-4}$  (measured  $(3.0 \pm 0.5) \times 10^{-4}$ )

They also show that a clock on Sirius B loses 1 s per hour.

### [17.2] Intervals & Geodesics / p 622

Point in spacetime  $(x, y, z, t) = \text{event}$

Field equations  $\mathcal{G} = -\frac{8\pi G}{c^4} \tilde{T}$

$\tilde{T} = 4 \times 4$  stress-energy tensor, with components equal to fluxes of mass/energy/momentum in the different directions.

$\mathcal{G} =$  Einstein tensor describes curvature of spacetime via derivatives of metric tensor.

So - curvature of spacetime caused by energy-momentum densities & fluxes.

### p. 623 Worldlines & World Cones

(Fig. 17.12 p 623) Spacetime diagrams ( $z$  suppressed) - man sleeping on couch, woman running to a sale, satellite orbiting Earth.

(Fig. 17.13 p 624) Event A = flashbulb set off at origin at  $t=0$ .  
Worldlines of photons in  $xy$  plane = light cone ( $45^\circ$  wr proper scaling).  
Massive particle  $v < c \Rightarrow$  inside lightcone = future of A = everything that could be caused by A.

Inside lower light = part of A = set of events that could cause A.

Outside the lightcones = elsewhere of A - region of spacetime completely inaccessible to us. Example: California, right now. We can influence CA in the future, it can influence us in the future, but not now.

Your destiny, your entire future worldline, must lie within your future lightcone.

### p 624 Spacetime Intervals, Proper Time, & Proper Distance

In flat 3D space, the distance  $\Delta l$  between 2 points is given by  
 $(\Delta l)^2 = \Delta x^2 + \Delta y^2 + \Delta z^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2$ , & is invariant under translation & rotation.

In flat spacetime, the (spacetime) interval  $\Delta s$  is given by  
 $\Delta s^2 = [c(t_2 - t_1)]^2 - (x_2 - x_1)^2 - (y_2 - y_1)^2 - (z_2 - z_1)^2 = (\text{distance traveled by light in } |t_2 - t_1|)^2 - (\text{distance between events A & B})^2$ , & is invariant under Lorentz transformations.

If  $(\Delta s)^2 > 0 \Rightarrow$  timelike  $\Rightarrow$  events causally related.

$\exists$  inertial frame which moves from one event to other, so  $\Delta x = 0$   
 so proper time interval  $\Delta \tau = \frac{\Delta s}{c}$  (proper time measured by clock  
 present at both events). (Fig. 17.14 p. 626)

If  $(\Delta s)^2 = 0$ , interval is lightlike or null,  $\Delta \tau = 0$

If  $(\Delta s)^2 < 0 \Rightarrow$  spacelike  $\Rightarrow$  not causally related. Can find frames in  
 which  $\Delta t < 0$ ,  $> 0$ , or  $= 0$ .

Proper distance (length) = (distance between events in frame in which  
 $\Delta t = 0$ ) =  $\Delta L = \sqrt{-(\Delta s)^2}$  in this case.

$(\Delta s)^2 < 0, = 0, \text{ or } > 0 \Rightarrow$  event is outside, on, or inside lightcone.

### p626 The Metric for Flat Spacetime

Flat 3D space  $\Rightarrow$  differential distance formula = metric:  $(dl)^2 = (dx)^2 + (dy)^2 + (dz)^2$

Distance along path  $P = \Delta L = \int_1^2 \sqrt{(dl)^2} = \int_1^2 \sqrt{(dx)^2 + (dy)^2 + (dz)^2}$

Similarly, for flat spacetime, the interval along worldline  $\mathcal{W}$  is

$$\Delta s = \int_A^B \sqrt{(ds)^2} = \int_A^B \sqrt{(cdt)^2 - (dx)^2 - (dy)^2 - (dz)^2}$$

Proper time along curved worldline =  $\Delta s/c$  ( $(\Delta s)^2 > 0$ ),  $= 0$  ( $(\Delta s)^2 = 0$ )

Undefined (or imaginary) for  $(\Delta s)^2 < 0$ . (= time measured by watch  
 moving along worldline)

Compare  $\Delta s$  for 2 world lines connecting events  $A$  &  $B$ , both of  
 which occur at the origin of an inertial frame. (Fig. 17.15 p. 628)

For the straight line  $A \rightarrow B$ ,  $dx = dy = dz = 0$

$$\Delta s(A \rightarrow B) = \int_A^B \sqrt{(cdt)^2 - (dx)^2 - (dy)^2 - (dz)^2} = \int_A^B c dt = c(t_B - t_A)$$

On lines  $AC$  &  $CB$ ,  $\frac{dx}{dt} = v_{AC}$  &  $v_{CB}$  respectively, so  $\Delta s(A \rightarrow C \rightarrow B)$

$$= \int_A^C \sqrt{(cdt)^2 - (v_{AC} dt)^2} + \int_C^B \sqrt{(cdt)^2 - (v_{CB} dt)^2}$$

$$= (t_C - t_A) \sqrt{c^2 - v_{AC}^2} + (t_B - t_C) \sqrt{c^2 - v_{CB}^2} < c(t_C - t_A) + c(t_B - t_C) = \Delta s(A \rightarrow B)$$

In spacetime, a straight line is the longest distance between 2 events

This represents the twin paradox:  $AB$  is the worldline of the Earthbound  
 twin,  $ACB$  is the twin who travels to a distant star & then returns

Each twin measures their proper time as  $\Delta s/c$ : Earthbound twin  
 ages more.

### p628 Curved Spacetime & the Schwarzschild Metric

"straightest possible worldline" between events = geodesic.

Flat spacetime: geodesic = straight line. In curved spacetime it is curved.

Paths followed by freely-falling objects are geodesics, & these are  
 maxima, minima, or inflection points (compared to other worldlines  
 connecting the 2 events).

In flat spacetime we have  $(ds)^2 = (cdt)^2 - (dl)^2 = (cdt)^2 - (dr)^2 - (r d\theta)^2 - (r \sin\theta d\phi)^2$

In the vicinity of a spherical mass, this metric is changed,



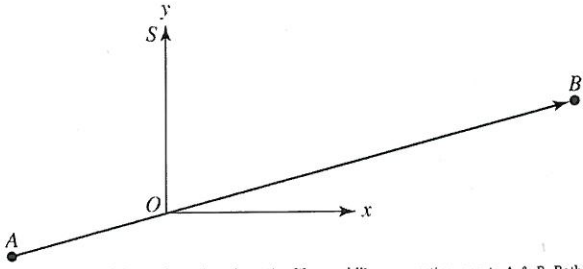


Fig. 17.14 Inertial frame  $S$  moving along timelike worldline connecting events  $A$  &  $B$ . Both events occur at origin of  $S$ .

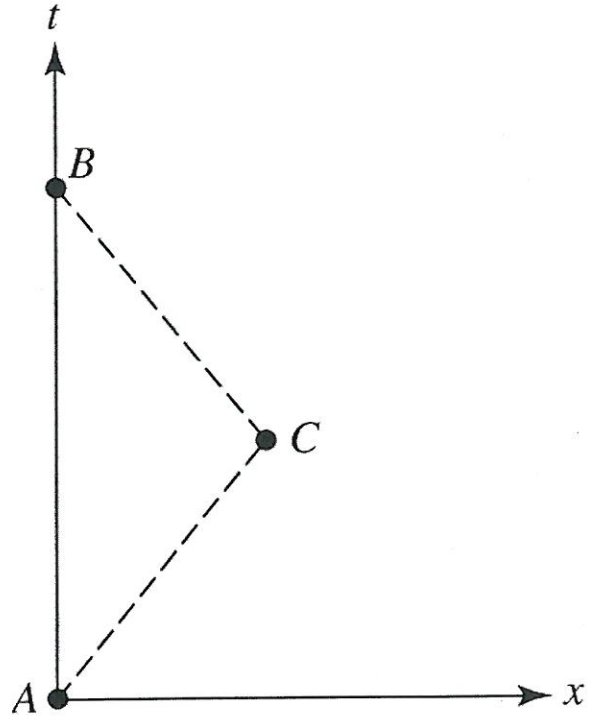


Fig. 17.15 Worldlines connecting events  $A$  &  $B$ .

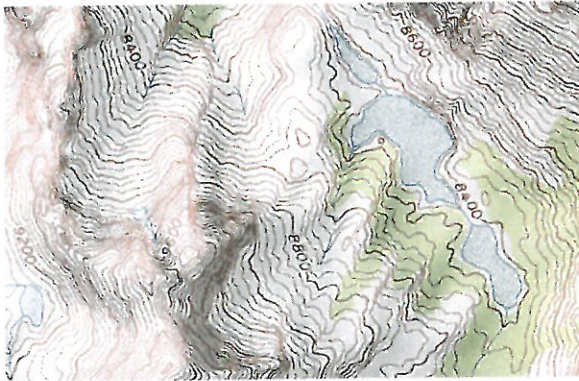


Fig. 17.16 Topographical map w/ elevation contour lines. Shortest distance between 2 points may not be straight line.

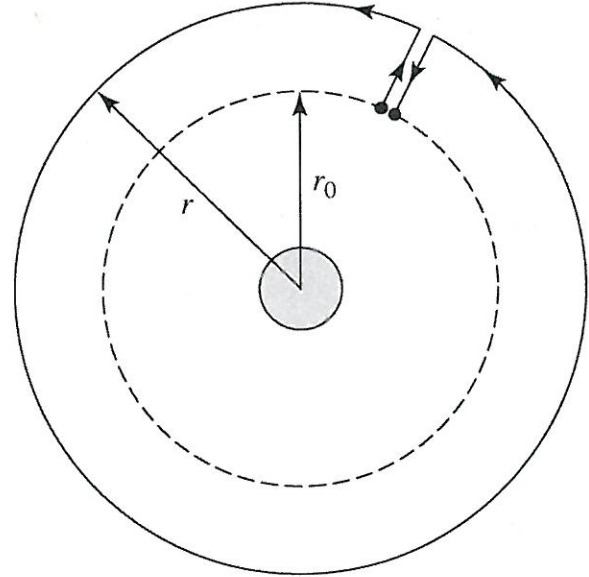


Fig. 17.17 "Orbit" of satellite, showing radial motions used to keep endpoints of worldline fixed. Net effect is circular orbit.



$(t, r, \theta, \phi)$  are coordinates measured by observer far from mass  $M$  (at  $\infty$ ).

There are problems with measuring  $r$  from the center of  $M$ , so instead use spheres centered at origin, define  $r$  by area  $= 4\pi r^2$ .

Coordinate speed = rate at which spatial coordinates change.

"In 1916, just 2 months after Einstein published his general theory of relativity, the German astronomer Karl Schwarzschild (1873-1916) solved Einstein's field equations to obtain what is now called the Sch. metric". (He died of a disease developed at the Russian front. He enlisted even though he was >40 yrs old.)

$$(ds)^2 = (c dt \sqrt{1 - 2GM/rc^2})^2 - \left(\frac{dr}{\sqrt{1 - 2GM/rc^2}}\right)^2 - (r d\theta)^2 - (r \sin\theta d\phi)^2$$

It is valid only outside the spherical mass distribution.

Proper distance measured at same time ( $dt=0$ ) between 2 points  $\forall r, d\theta = d\phi = 0$  is  $dL = \sqrt{-(ds)^2} = dr / \sqrt{1 - 2GM/rc^2} > dr$

Spatial distance  $> dr$  (Fig. 17.16 p631) Spatial distance  $>$  map distance.

Clock at rest at  $r$  measures proper time  $d\tau = \frac{ds}{c} = dt \sqrt{1 - \frac{2GM}{rc^2}} < dt$ .  
Time between ticks of clock as measured by observer at  $\infty = dt > d\tau$ .  
 $\Rightarrow$  gravitational time dilation.

### p. 631 The Orbit of a Satellite

Just! Newtonian:  $\frac{v^2}{r} = \frac{GM}{r^2} \Rightarrow v = \sqrt{\frac{GM}{r}}$

Circular orbit above equator:  $\theta = 90^\circ$ ,  $dr = d\theta = 0$ ,  $d\phi = \omega dt$

$$(ds)^2 = [c^2 \sqrt{1 - 2GM/rc^2}^2 - r^2 \omega^2] dt^2$$

$$\Delta S (1 \text{ orbit}) = \int_0^{2\pi/\omega} \sqrt{c^2 - \frac{2GM}{r} - r^2 \omega^2} dt$$

Variation must have fixed endpoints ( $r_0$ ), so use this path (Fig. 17.17 p633) to vary  $r$  (radial portions have negligible  $\Delta S$ )

$$\Rightarrow 0 = \frac{d}{dr} \sqrt{c^2 - \frac{2GM}{r} - r^2 \omega^2} \Rightarrow 0 = \frac{2GM}{r^2} - 2r\omega^2$$

$$\Rightarrow v = r\omega = \sqrt{\frac{GM}{r}} \quad \checkmark \quad \text{geodesic (Fig. 17.18 p634)}$$

This is true even for orbit around black hole.

### §17.3 Black Holes p. 633

Setting the classical escape velocity  $\sqrt{2GM/R}$  to  $c$  gives  $R = 2GM/c^2$ . Classically, not even light could escape from a star with such a small radius.  
The Schwarzschild Radius

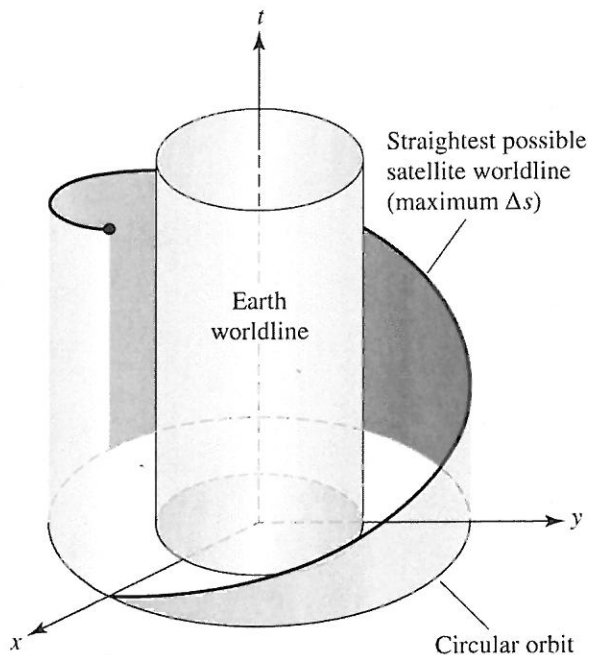


Fig. 17.18 Straightest possible worldline thru curved spacetime & its projection onto orbital plane of satellite.

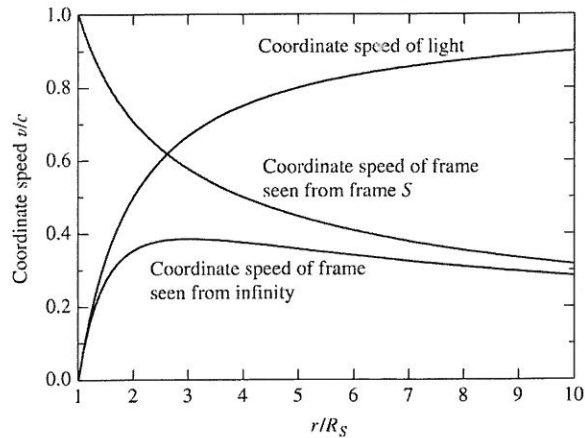


Fig. 17.19

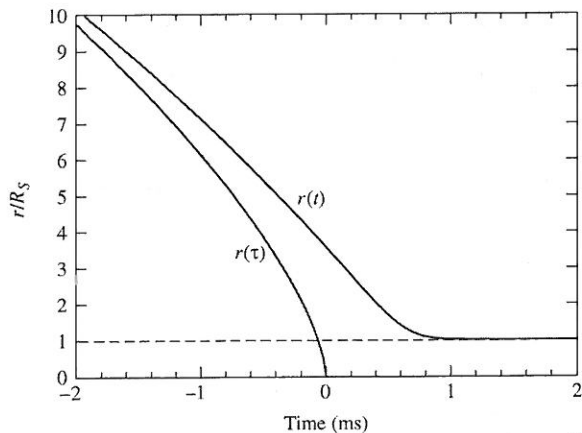


Fig. 17.20 Coordinate  $r(t)$  of freely falling frame  $S$  according to observer at rest at infinity, &  $r(\tau)$  according to observer in frame  $S$ . ( $R_S$  for  $10 M_{\odot}$  black hole.)

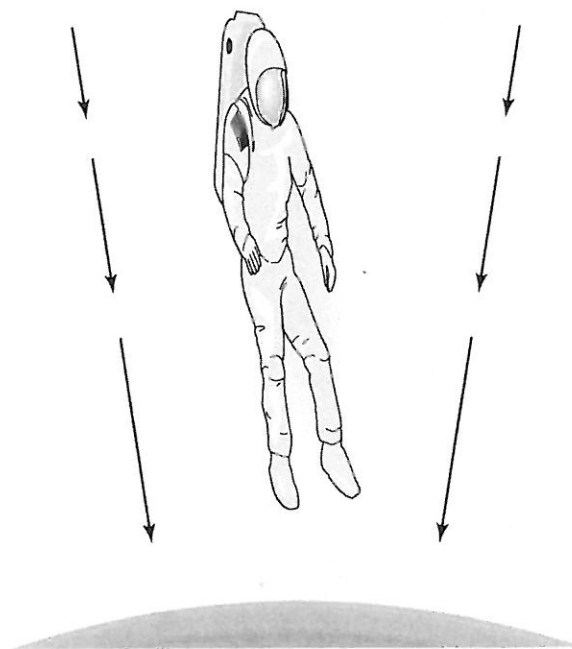


Fig. 17.21 Tidal forces near black hole.



This radius, called the Schwarzschild radius, is also the radius at which the  $\sqrt{1-2GM/rc^2}$  terms in the Schwarzschild metric  $\rightarrow 0$ .

$$R_s = 2GM/c^2 = 2.95 (M/M_\odot) \text{ km}$$

Lots of strange things happen near  $r=R_s$ .

Eq. 17.24:  $dt = d\tau / \sqrt{1-2GM/rc^2} = d\tau / \sqrt{1-R_s/r}$

$d\tau$  is proper time of clock at  $r$ ,  $dt$  = time measured by distant observer  $\rightarrow \infty$ .

Fig 17.19 p 636

Time is frozen at  $r=R_s$ !

Coordinate speed of light:  $ds = d\theta = d\phi = 0 \Rightarrow \frac{dr}{dt} = c(1 - \frac{R_s}{r}) = c(1 - \frac{R_s}{r}) \rightarrow 0$

Nothing can be seen from within  $r=R_s$  - the event horizon of the black hole. At the (unobservable) center of a bh is the singularity - a point of infinite density + curvature of spacetime. (QM may smear this out to a size  $\sim$  Planck length  $l_p = \sqrt{\frac{\hbar G}{c^3}} = 1.6 \times 10^{-35} \text{ m}$ .)

Law of Cosmic Censorship: no naked singularities - unclothed - without event horizon.

p 636 A Trip into a Black Hole

Time for a photon to travel out from  $r_1$  to  $r_2 > r_1$ :

$\Delta t = \int_{r_1}^{r_2} \frac{dr}{c \sqrt{1-R_s/r}} = \int_{r_1}^{r_2} \frac{r dr}{c(r-R_s)} = \int_{r_1}^{r_2} \frac{r-R_s+R_s}{c(r-R_s)} dr = \int_{r_1}^{r_2} (\frac{1}{c} + \frac{R_s}{c(r-R_s)}) dr$   
 $= [\frac{r}{c} + \frac{R_s}{c} \ln(r-R_s)]_{r_1}^{r_2} = \frac{r_2-r_1}{c} + \frac{R_s}{c} \ln(\frac{r_2-R_s}{r_1-R_s})$ , For  $r_1=R_s$ ,  $\Delta t = \infty$ .

This is true for a photon coming out from  $r_1=R_s$  or inwards from  $r_1=\infty$ .

So a bh is a frozen star - even the surface of the star that formed it appear to be at the event horizon.

What if an astronaut decided to free-fall into a  $10 M_\odot$  ( $R_s = 30 \text{ km}$ ) bh? Observer at  $\infty$  sees her slowing down as she approaches  $R_s$ , her motions become slow, she emits fewer + fewer photons, which are more + more redshifted.

(Fig 17.20 p 637)

From her perspective, tidal forces stretch her in the radial direction + squeeze her laterally. (Fig. 17.21 p 638)

She falls through the event horizon + is crushed in the singularity  $\Delta t = 6.6 \times 10^{-5} \text{ s}$

It is impossible to be at rest at  $r=R_s$ :  $dr = d\theta = d\phi = 0 \Rightarrow$

$$(ds)^2 = (cdt)^2 (1 - \frac{R_s}{r}) < 0 \text{ (spacelike interval, not permitted for particles)}$$

p. 639 Mass Ranges of Black Holes

Stellar-mass bhs:  $M = 3-15 M_\odot$  (core collapse of supergiant star)

Intermediate-mass bhs: IMBHs:  $M = 100 \rightarrow 1000$  or  $10^4 M_\odot$  (maybe from merger of stellar-mass bhs)

Super-massive bhs (SMBHs) exist at centers of most galaxies:  $10^5 - 10^9 M_\odot$   
 (MW BH =  $3.7 \pm 0.2 \times 10^6 M_\odot$ ). Formation model still unclear.

Primordial BHs formed in BB,  $10^{-8} \text{ kg} - 10^5 M_\odot$

(2015 Grav wave -  $M = 29 + 36 M_\odot$  bh merger)

Ex. 17.31  $R_s$  (Earth) =  $0.009 \text{ m} = 9 \text{ mm}$

p 640 BHs Have No Hair!

Any irregularities in shape of BH quickly radiated away as grav. waves. BH can be completely described by  $M, L, + Q$



$L_{\max} = \frac{GM^2}{c}$  for bh:  $L > L_{\max} \Rightarrow$  naked singularity.

Ex. 17.3.2 For sun,  $L_{\max, \odot} = GM_{\odot}^2/c = 8.81 \times 10^{41} \text{ kg m}^2 \text{ s}^{-1}$

$L_{\odot} = 1.63 \times 10^{41} \text{ kg m}^2 \text{ s}^{-1} = 0.18 L_{\max, \odot} \Rightarrow L \hat{=} L_{\max}$  should be common for stellar-mass bh's.

### p. 640 Spacetime Frame Dragging

BH w/  $L \neq 0$  not spherically symmetric  $\Rightarrow$  described by Kerr (Roy Kerr, 1963) metric, not Schwarzschild. (why do my d-ms move outward when I rotate?)

Rotating bh (or other object) induces rotation in surrounding spacetime  $\Rightarrow$  frame dragging: an inertial frame rotates.

(Fig. 17.22 p. 641) In ergosphere all particles must move in same direction as bh rotation. Outer limit of ergosphere = static limit  $\Rightarrow$  particles can stand still.

### part. p. 642 - Tunnels in Spacetime (Fig. 17.23 p. 642)

Einstein-Rosen bridges + wormholes connecting 2 distant parts of spacetime are theoretically possible but require exotic unknown matter/energy to keep them open + stable.

Also, wormholes may be impossible (Stephen Hawking says) because they would allow time travel to the past.

### part. p. 643 Stellar-Mass BH Candidates

The best chance of observing stellar-mass bh's is when they are accreting matter from a normal binary companion. (Fig. 17.24 p. 644)

Normal companion evolves, expands, overflows its Roche lobe, forms accretion disk, gas is compressed + heated to millions of K, emits X-rays.

Most of these binary X-ray sources are nsr, but if  $M \geq 3M_{\odot}$ , it's a BH.

1st candidate = Cygnus X-1. Also LMC X-3,

A0620-00:  $M \geq 3.82 \pm 0.24 M_{\odot}$

V404 Cygni -  $M = 12 \pm 2 M_{\odot}$

### p. 644 Hawking Radiation

Stephen Hawking (1974): BH's evaporate.

Virtual particle-antiparticle pair created just outside event horizon, one falls in before they can recombine, so a particle is emitted + the BH's mass decreases. (Fig. 17.25 p. 645)

It is as if a BH emits thermal radiation with  $T \propto \frac{1}{M}$ , emission rate  $\propto R^2 T^4 \propto M^2 M^{-4} \propto M^{-2}$

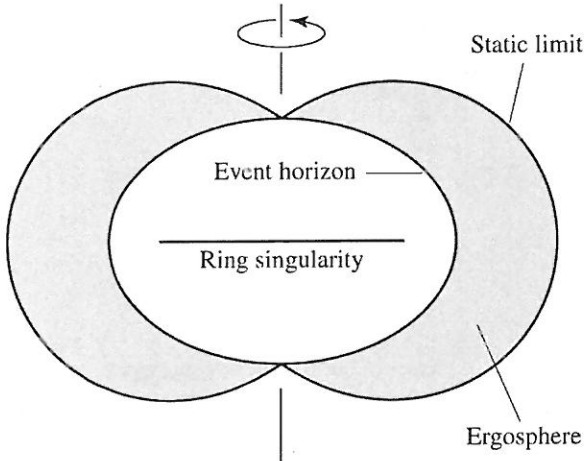


Fig. 17.22 Maximally rotating black hole, w/ ring singularity seen edge-on. Event horizon at equator is  $r = \frac{1}{2}R_s$ .

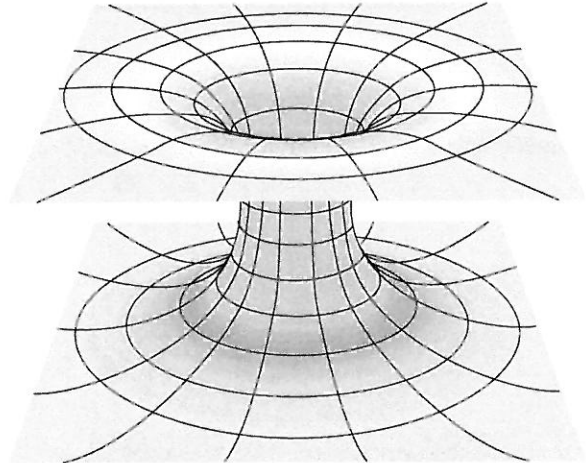


Fig. 17.23 Schwarzschild throat connecting 2 regions of spacetime.

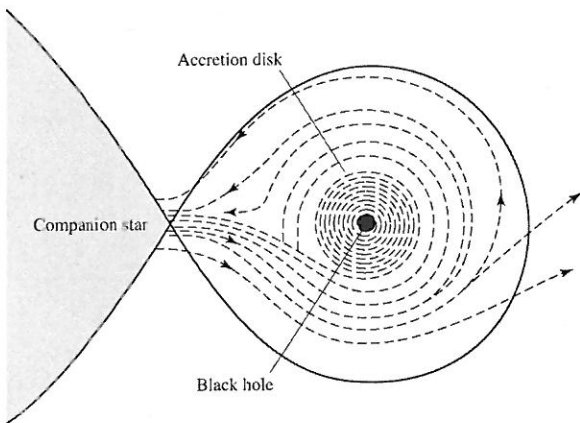


Fig. 17.24 Gas pulled from companion star forms X-ray emitting disk around black hole.

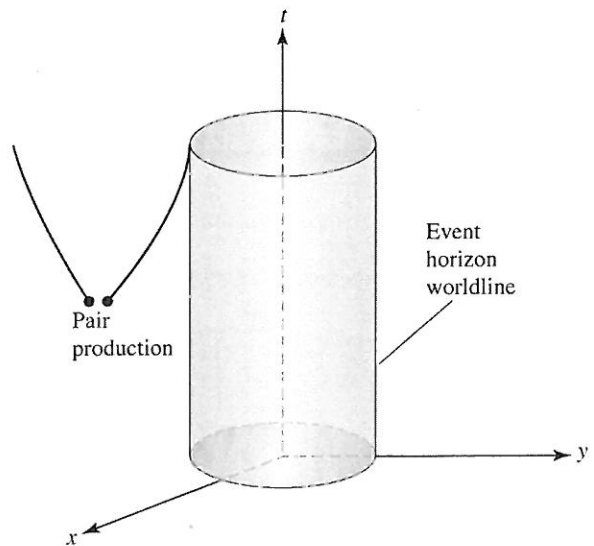


Fig. 17.25 Particle-antiparticle pairs created near event horizon of black hole.

40c

2/18/18

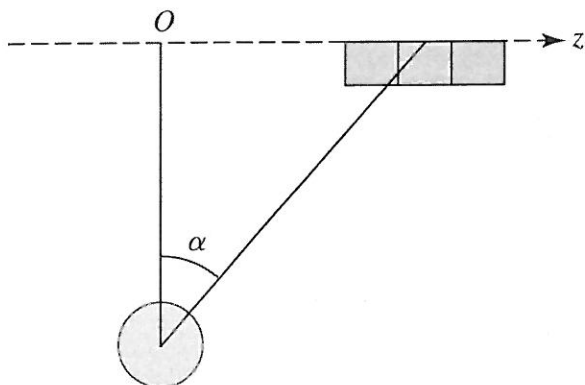


Fig. 17.26 Local inertial frames for measuring deflection of light near Sun.



Evaporation time  $\propto M / \text{rate} \propto M^3$   
 $t_{\text{evap}} = 2560 \pi^2 \left( \frac{2GM}{c^2} \right)^2 \left( \frac{M}{h} \right) \approx 2 \times 10^{67} \left( \frac{M}{M_{\odot}} \right)^3 \text{ yr}$

Age of universe  $\sim 13.7$  billion years.

Primordial BH wr  $M \sim 1.7 \times 10^{11} \text{ kg}$  should evaporate  $\sim$  now.

Final evaporation is explosive, releasing  $\sim 100 \text{ MeV}$   $\gamma$ 's at  $10^{13} \text{ W}$ , also other particles.

Non-detection  $\Rightarrow < 200$  BHs wr this mass per cubic light year.

## Ch. 18 Close Binary Star Systems - p 653

### §18.6 NSs & BHs in Binaries p 689

If star in close binary undergoes SN, result may be ns or bh in binary.  
 In semidetached system (Fig. 18.4), hot gas flows through inner Lagrangian point from companion star onto compact object.

Gravitational energy  $\rightarrow$  X-rays.

It is also possible to have 2 compact objects in binary system.

### Formation of Binaries with Neutron Stars or Black Holes

Binary system survives SN of one star if ejected mass small enough.

Simple model: stars in circular orbits, spherically symmetric SN.

Can show (Prob. 18.17) that the system will be unbound ( $E_T \geq 0$ )

if the remnant mass satisfies  $\frac{M_R}{M_1 + M_2} \leq \frac{1}{(2 + M_2/M_1)(1 + M_2/M_1)} < \frac{1}{2}$

(Star 1 explodes)

### p. 690 Capturing Isolated Neutron Stars

In order for a ns to form a binary in an encounter wr another star, energy must be dissipated.

Passing ns raises tidal bulges on nearby normal star  $\Rightarrow$  tidal capture.

Most effective in region densely populated wr stars - globular clusters.

In fact, there are lots of X-ray sources in globular clusters.

Or a ns can be captured by a system containing  $\geq 2$  stars - one is ejected, removing energy from the system.

### p. 691 - Binary X-ray Pulsars

1<sup>st</sup> discovered extrasolar X-ray source = Sro X-1 = binary X-ray pulsar.

Atmosphere opaque to X-rays, so must use balloon, rocket, or satellite.

Grav. energy  $\sim 0.2 mc^2$  ( $\gg E_{\text{nuc}}$ )

$L_x \leq L_{\text{Ed}} \sim 10^{31} \text{ W}$ ,  $T \sim 2 \times 10^7 \text{ K}$  ( $\lambda_{\text{max}} \sim 0.15 \text{ nm} \Rightarrow$  X-rays)